

# Modelling buoyancy effects in the coastal zone

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- Mixing vs. stratification
- General Ocean turbulence Model (GOTM)
- Example: SIPS in Liverpool Bay
- Tidal asymmetry & residual transport
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- Can this be relevant for the Wadden Sea ?
- Dynamics of dense bottom plumes
- Example: Influx events in Arkona Sea

# $k$ - $\varepsilon$ model I

Turbulent Fluxes (velocity & temperature):

$$\langle \tilde{u}\tilde{w} \rangle = -\nu_t \partial_z \bar{u}, \quad \langle \tilde{w}\tilde{T} \rangle = -\nu'_t \partial_z \bar{T}$$

Eddy Viscosity / Eddy Diffusivity:

$$\nu_t = c_\mu \frac{k^2}{\varepsilon}, \quad \nu'_t = c'_\mu \frac{k^2}{\varepsilon}.$$

$k$ : Turbulent kinetic energy (TKE) [J/kg]

$\varepsilon$ : Dissipation of TKE [W/kg]

# $k$ - $\varepsilon$ model II

$k$ - $\varepsilon$  model (*Launder and Spalding [1972]*):

$$\partial_t k - \partial_z \left( \frac{\nu_t}{\sigma_k} \partial_z k \right) = P + B - \varepsilon,$$

$$\partial_t \varepsilon - \partial_z \left( \frac{\nu_t}{\sigma_\varepsilon} \partial_z \varepsilon \right) = \frac{\varepsilon}{k} (c_{\varepsilon 1} P + c_{\varepsilon 3} B - c_{\varepsilon 2} \varepsilon).$$

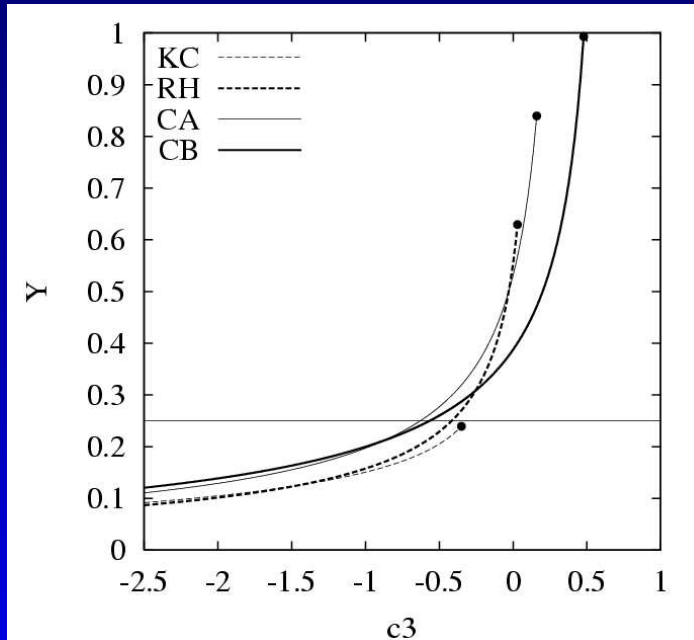
$P$ : Shear production of TKE [W/kg]

$B$ : Buoyancy production [W/kg]

# Total equilibrium ( $k$ - $\epsilon$ )

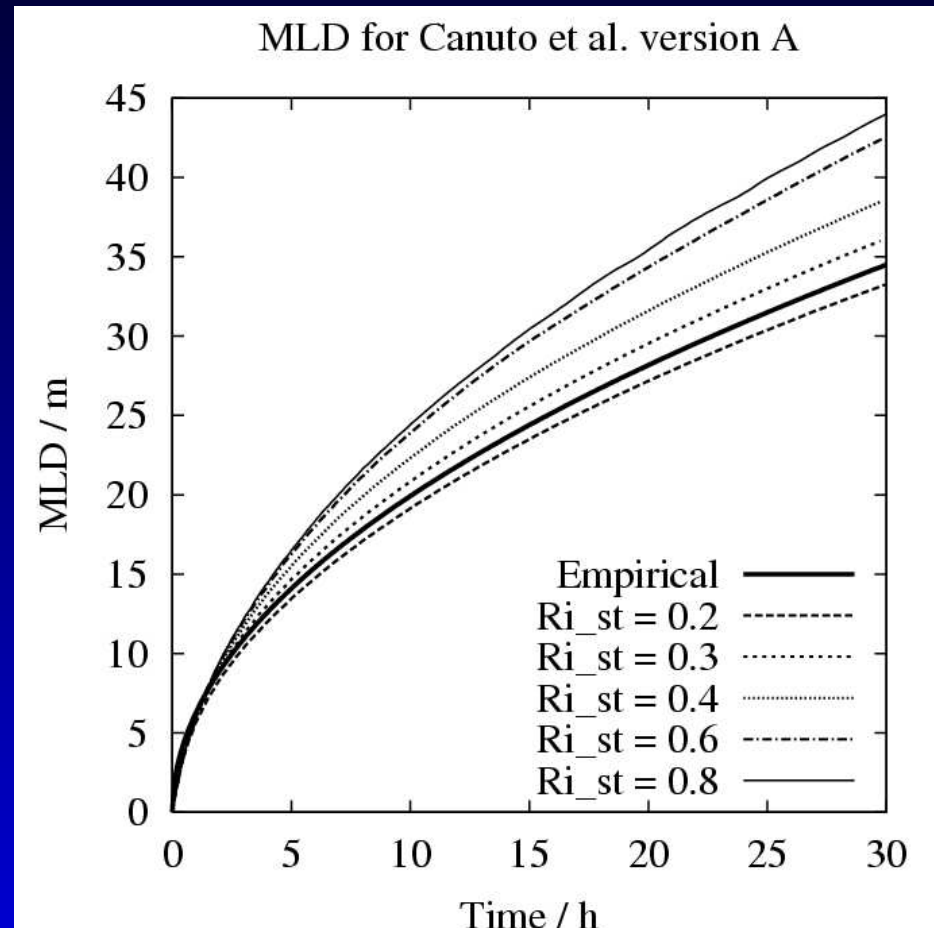
$$\dot{k} = \dot{\epsilon} \implies R_i = \frac{-\frac{g}{\rho_0} \partial_z \rho}{(\partial_z u)^2 + (\partial_z v)^2} = R_i^{st} = \frac{c_\mu}{c'_\mu} \cdot \frac{c_{2\epsilon} - c_{1\epsilon}}{c_{2\epsilon} - c_{3\epsilon}}.$$

$R_i^{st} \approx 0.25$ : Steady-state Richardson number.



# Kato-Phillips experiment

## Wind-induced mixed-layer depth (MLD)




Burchard & Bolding [2001]

GOTM (General Ocean Turbulence Model) - Microsoft Internet Explorer

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Address: http://www.gotm.net



**Challenge**


- [Aim](#)
- [The Idea](#)
- [Key features](#)

**Software**

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- [Test cases](#)
- [Forcing](#)
- [How to run?](#)

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19309 

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# General Ocean Turbulence Model

GOTM is a one-dimensional numerical model developed and supported by a [core team](#) of ocean modellers. GOTM aims at simulating accurately [vertical exchange processes](#) in the marine environment where [mixing](#) is known to play a key role. GOTM is freely available under the [GPL](#) (Gnu Public License).

If you are interested in using GOTM, you can download:

Software: [Fortran source](#)

Examples: [Test cases - Outputs](#)

Documentation: [Summary](#) - [2003 report](#) - [1999 report](#)

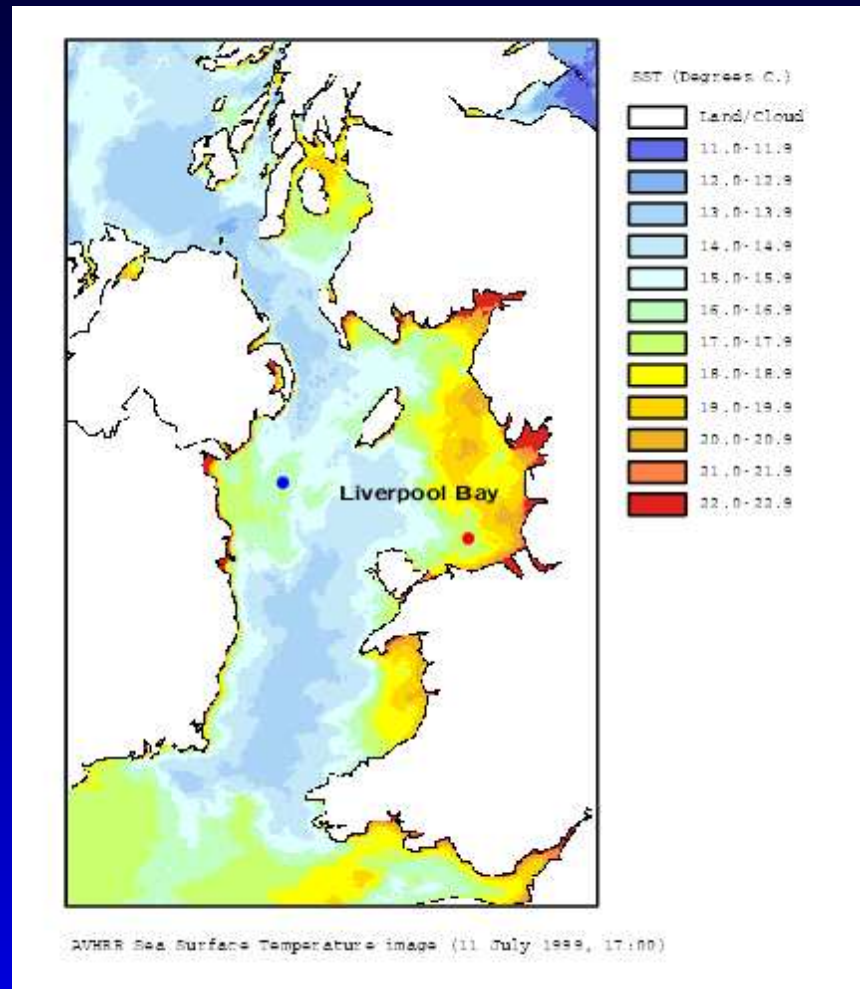
You are warmly invited to join the [GOTM mailing list](#) and send any comments/questions to the [GOTM developers](#) or become a [GOTM contributor](#). The GOTM developers are grateful to their [sponsors](#).

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Last updated: 03/16/2003 09:42:06

# Liverpool Bay

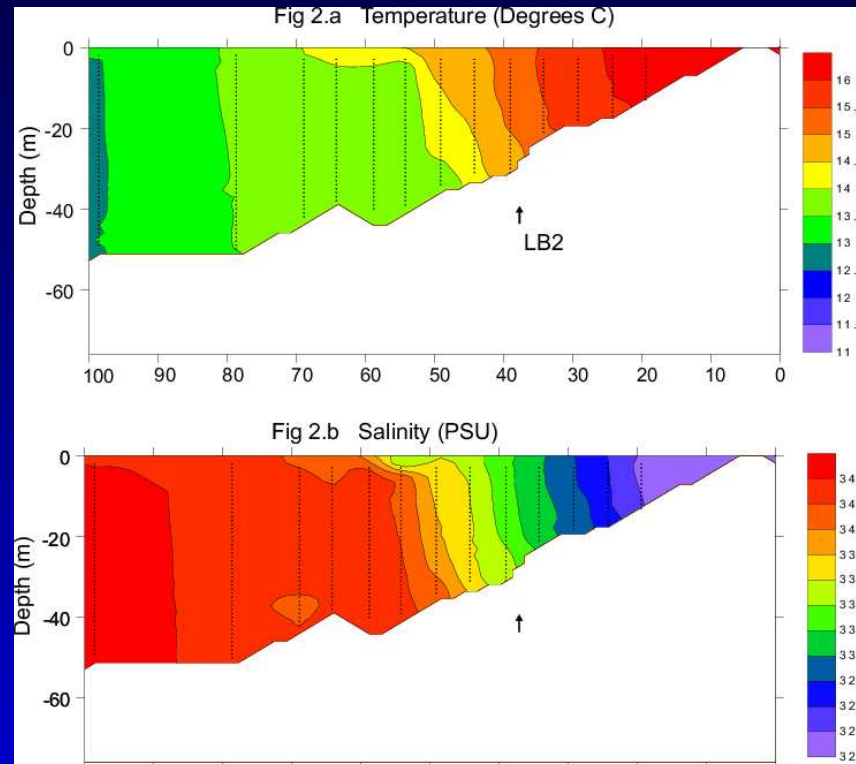
SST from space and location of station (●)



Courtesy to School of Ocean Sciences, UBW, Wales

# Liverpool Bay

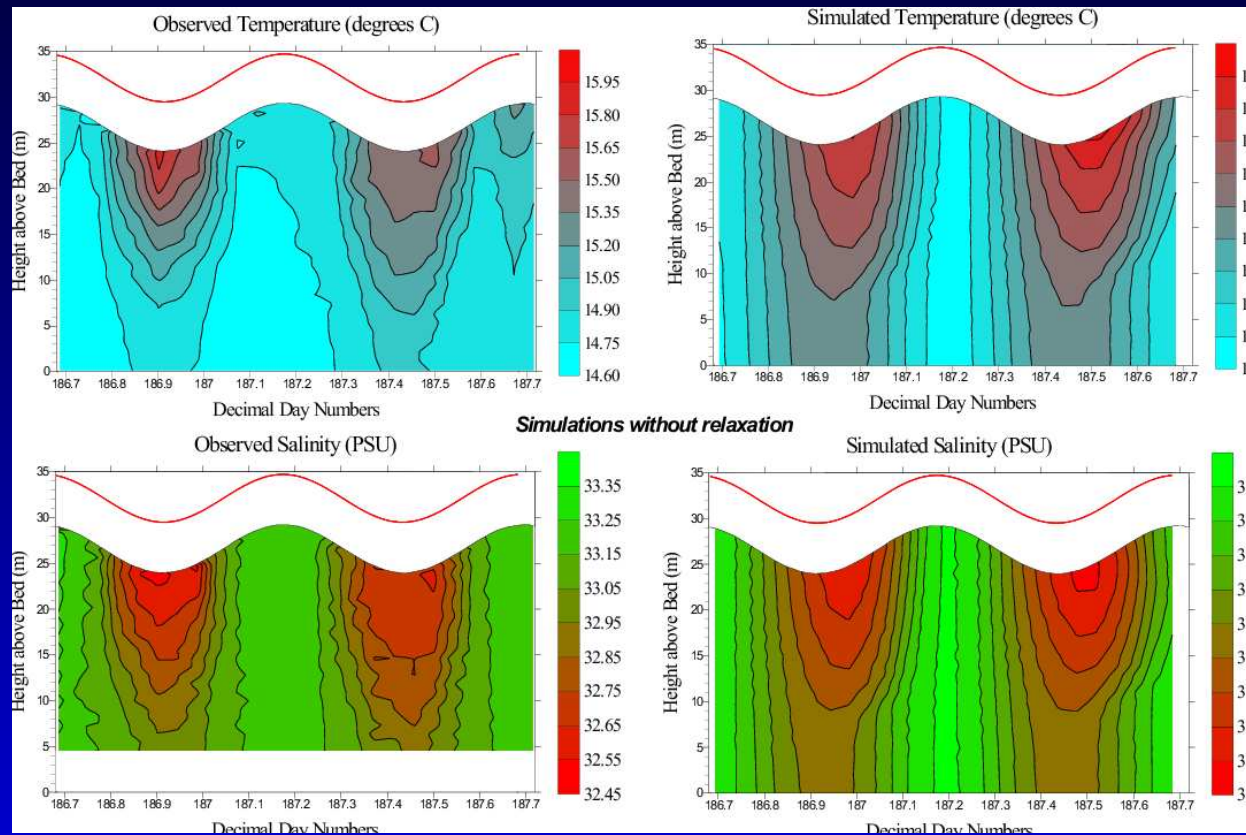
## Section of Temperature and Salinity



Rippeth, Fisher, Simpson [2001]

# Liverpool Bay

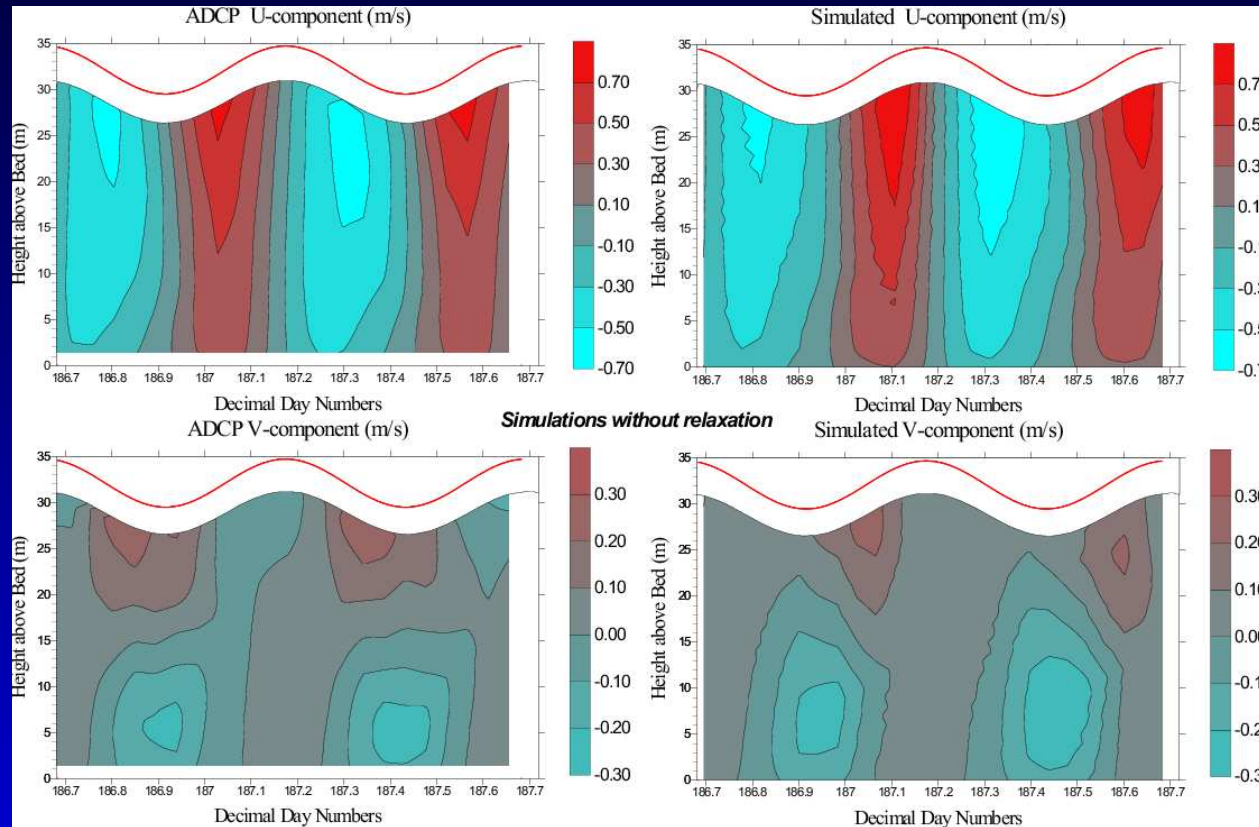
## Observed and simulated temperature and salinity



Simpson, Burchard, Fisher, Rippeth [2002]

# Liverpool Bay

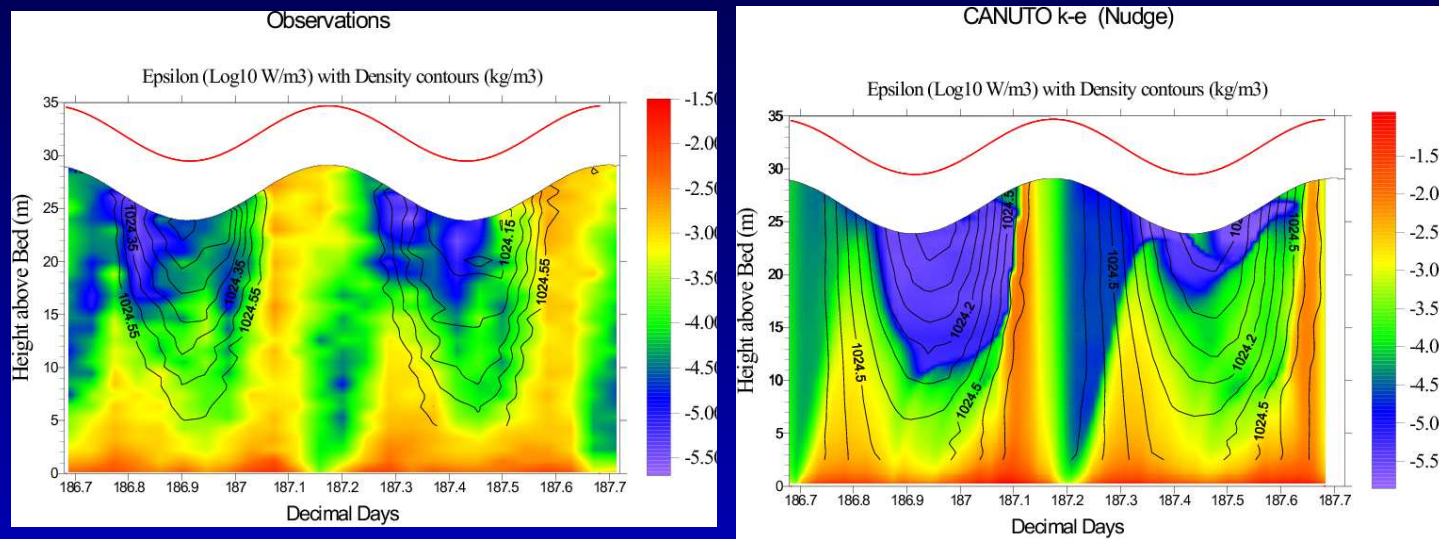
## Observed and simulated current velocity



Simpson, Burchard, Fisher, Rippeth [2002]

# Liverpool Bay

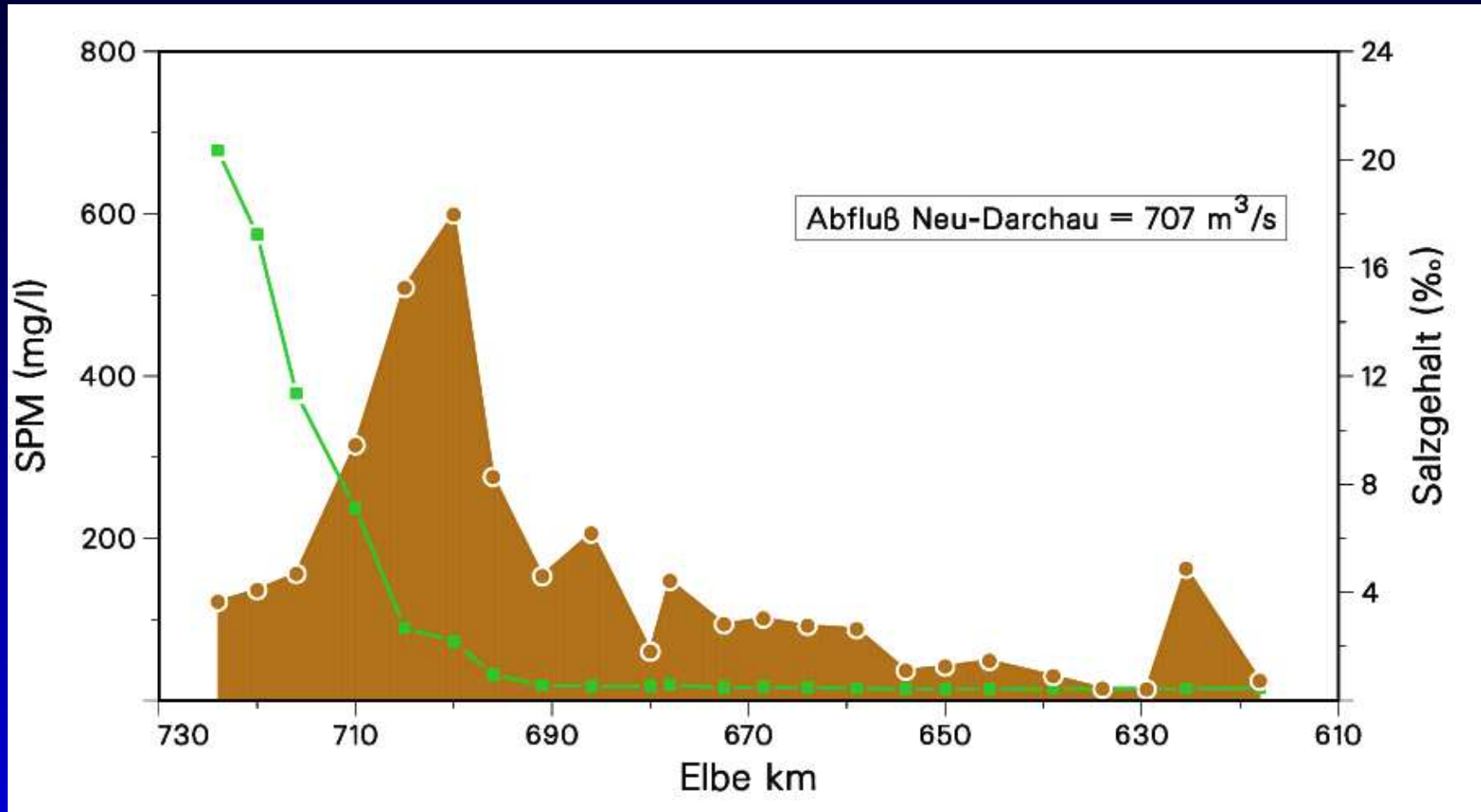
## Observed and simulated dissipation rates



Simpson, Burchard, Fisher, Rippeth [2002]

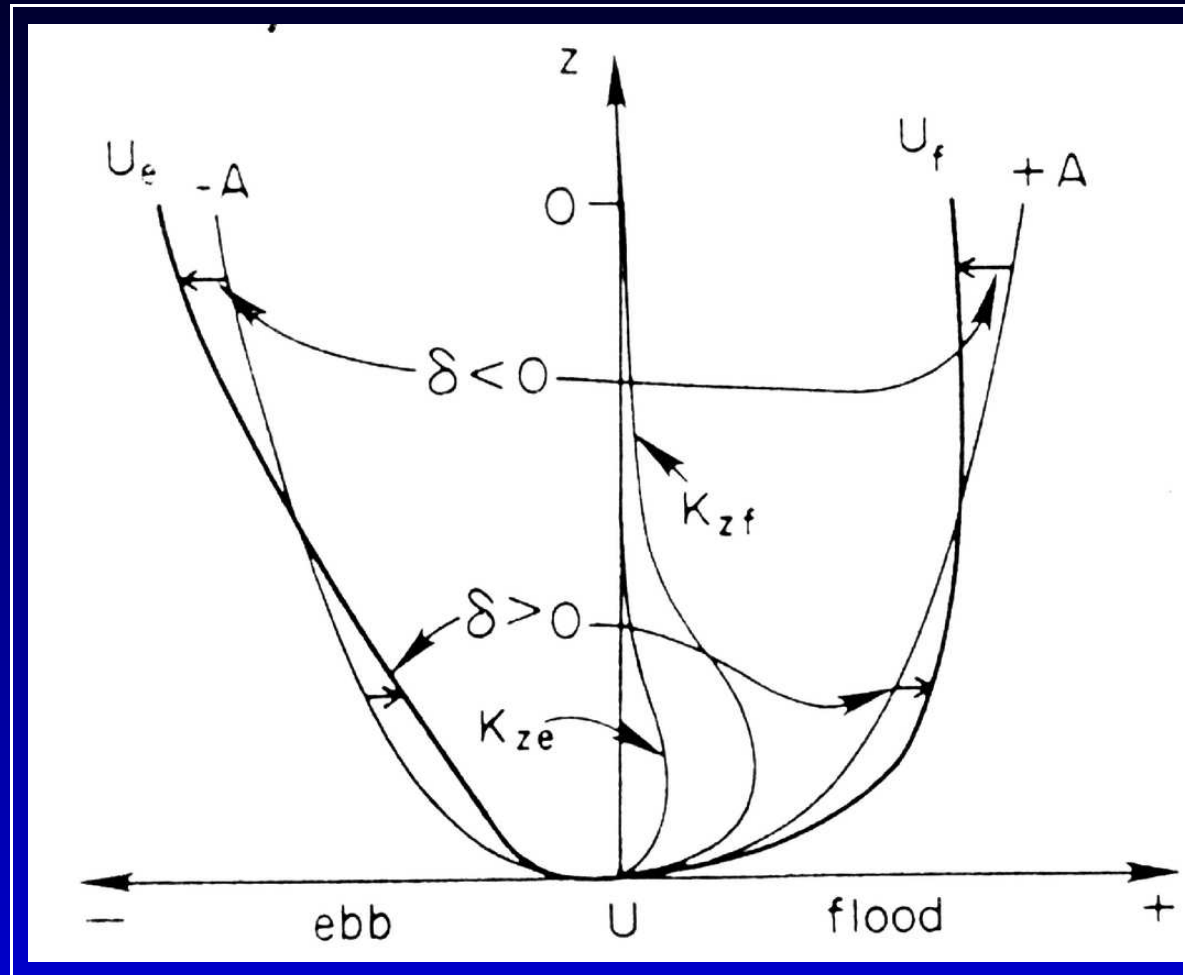
# Estuarine Turbidity Maximum

## SPM observations in the tidal Elbe



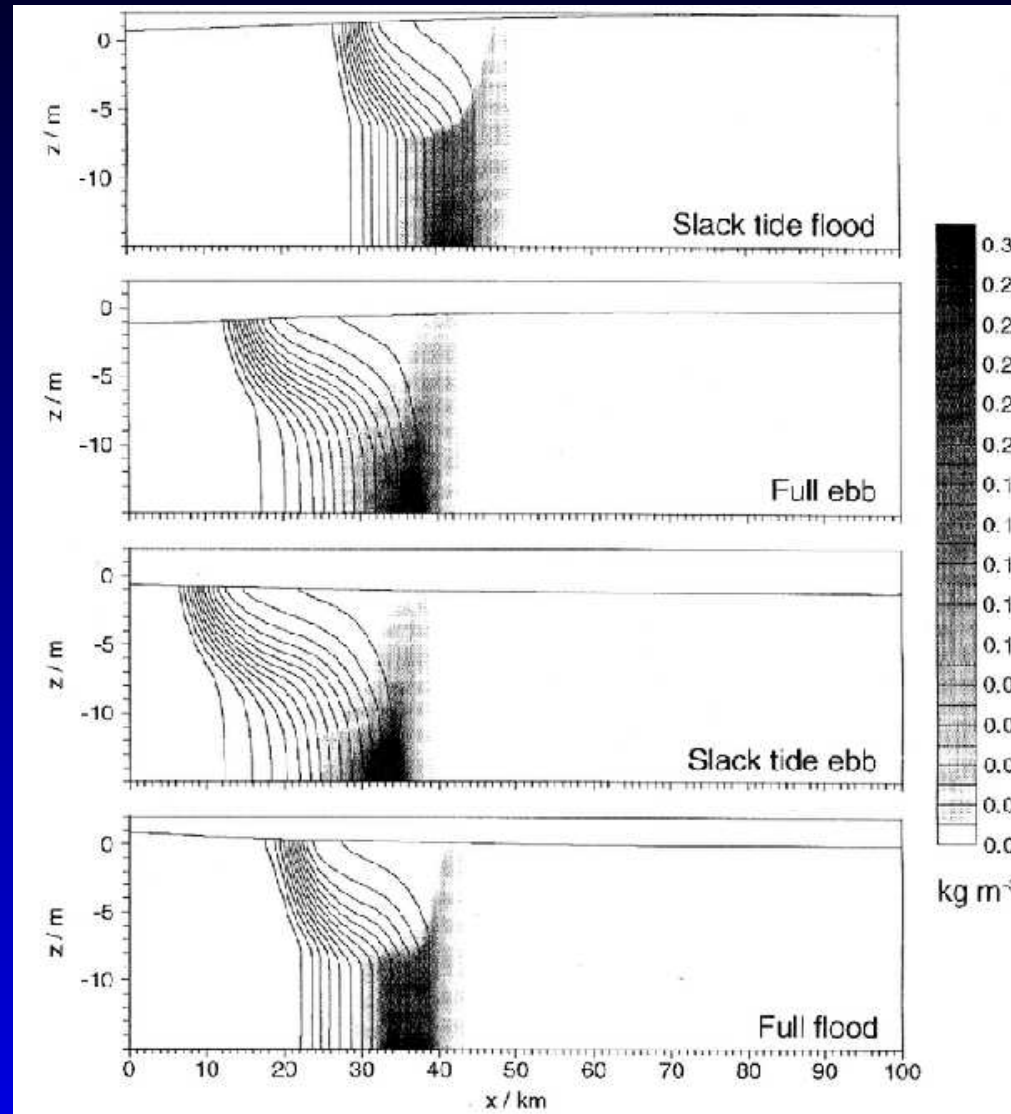
Pers. comm. Jens Kappenberg

# ETM: Conceptual model

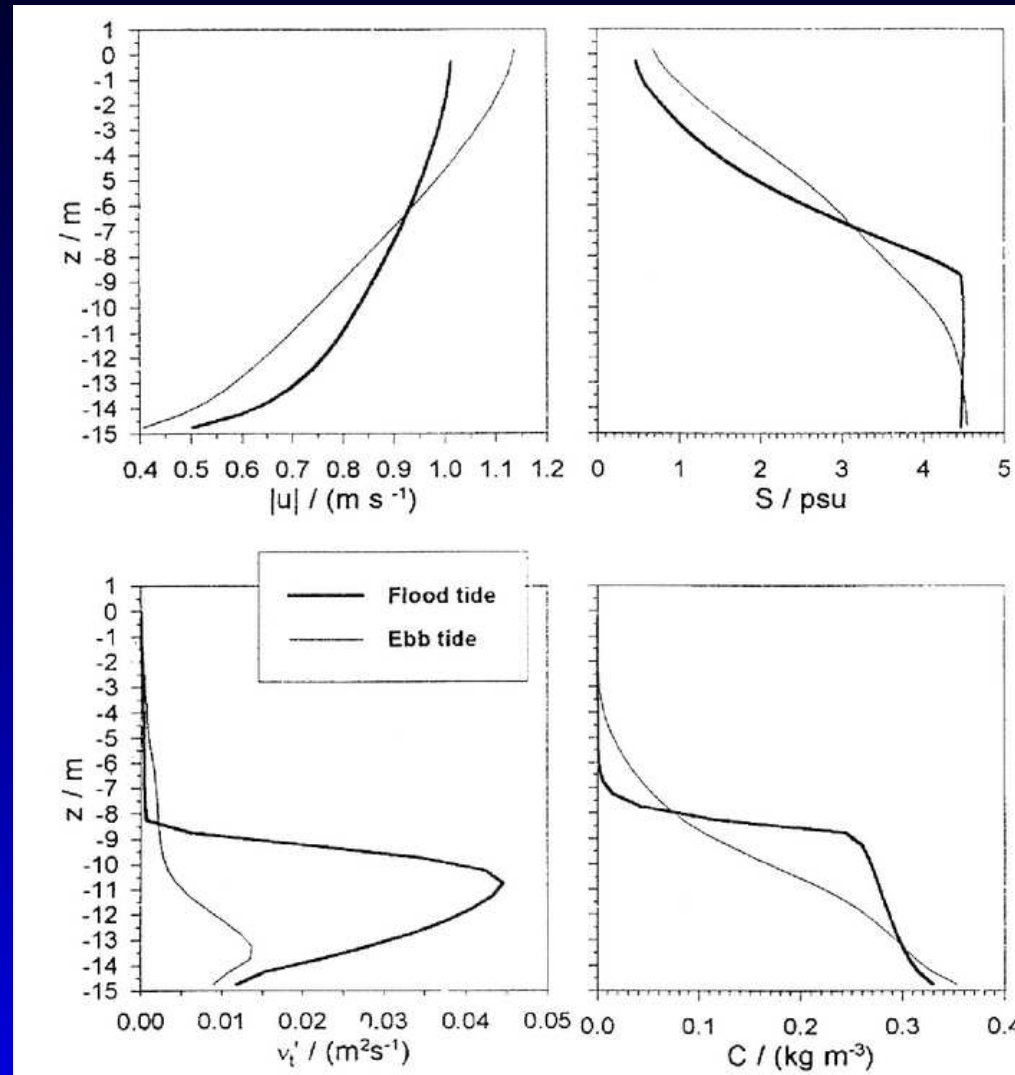


Jay & Musiak, 1994

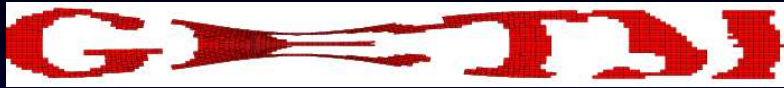
# ETM: Computer simulations



# ETM: Computer simulations



Burchard & Baumert, 1998



## General Estuarine Transport Model

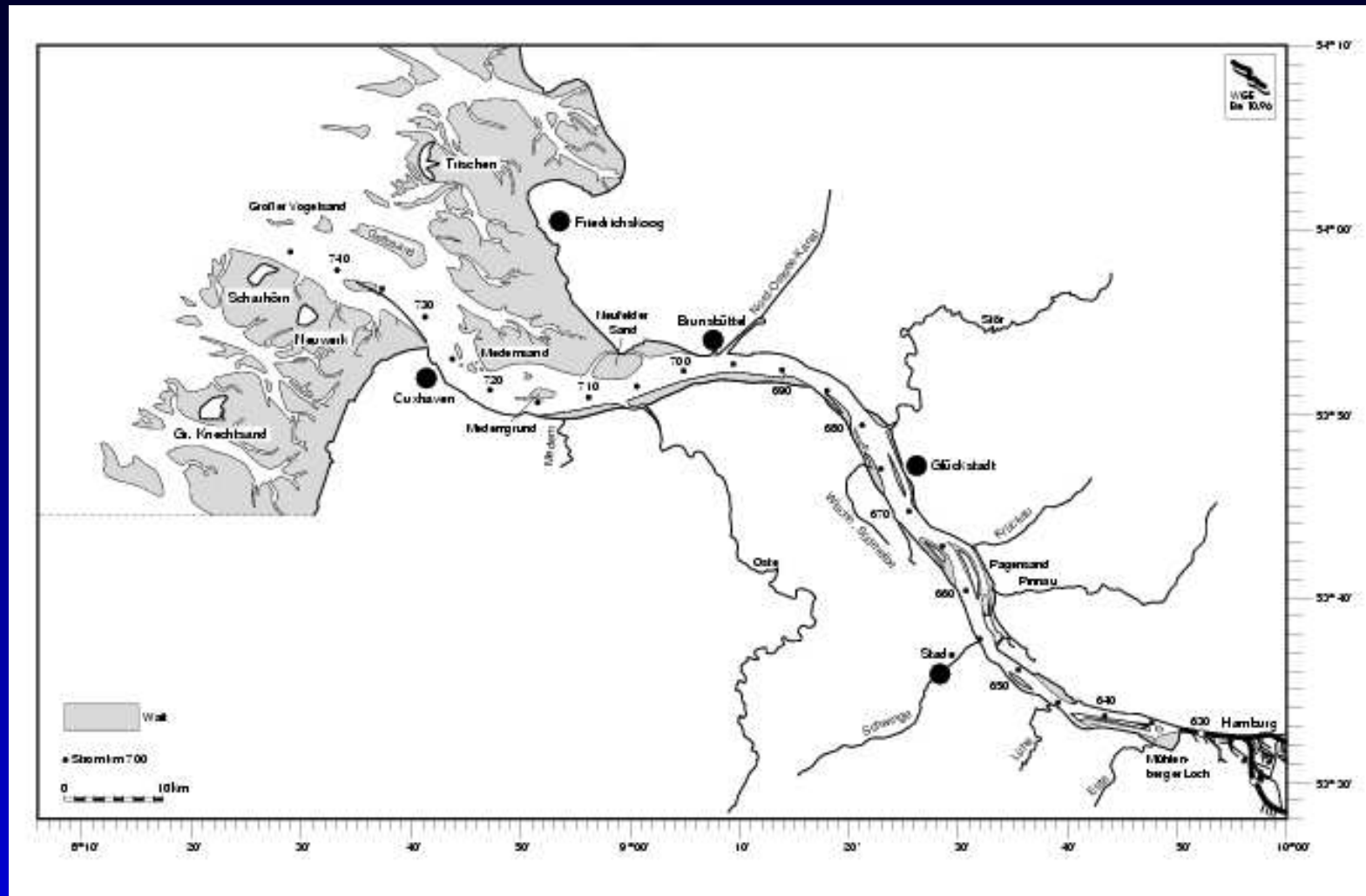
- Three dimensional, hydrostatic, free surface, baroclinic
- Mode-splitting, Arakawa-C grid
- Horizontal coord.: Cartesian, spherical or orthogonal
- Vertical coord.: Sigma, z-levels or generalised
- Turbulence closures from GOTM (<http://www.gotm.net>)
- Various advection schemes for momentum and tracers
- Stable drying and flooding algorithm
- Fully parallelised (domain decomposition)
- Public Domain (<http://www.bolding-burchard.com/getm>)

# 2D Experiments

- Salinity and SPM (click for animation), no advection of turbulence
- Salinity and eddy diffusivity (click for animation), no advection of turbulence

Burchard et al. [2004]

# Elbe-ETM in 3D: GETM



Animation

# Oosterschelde

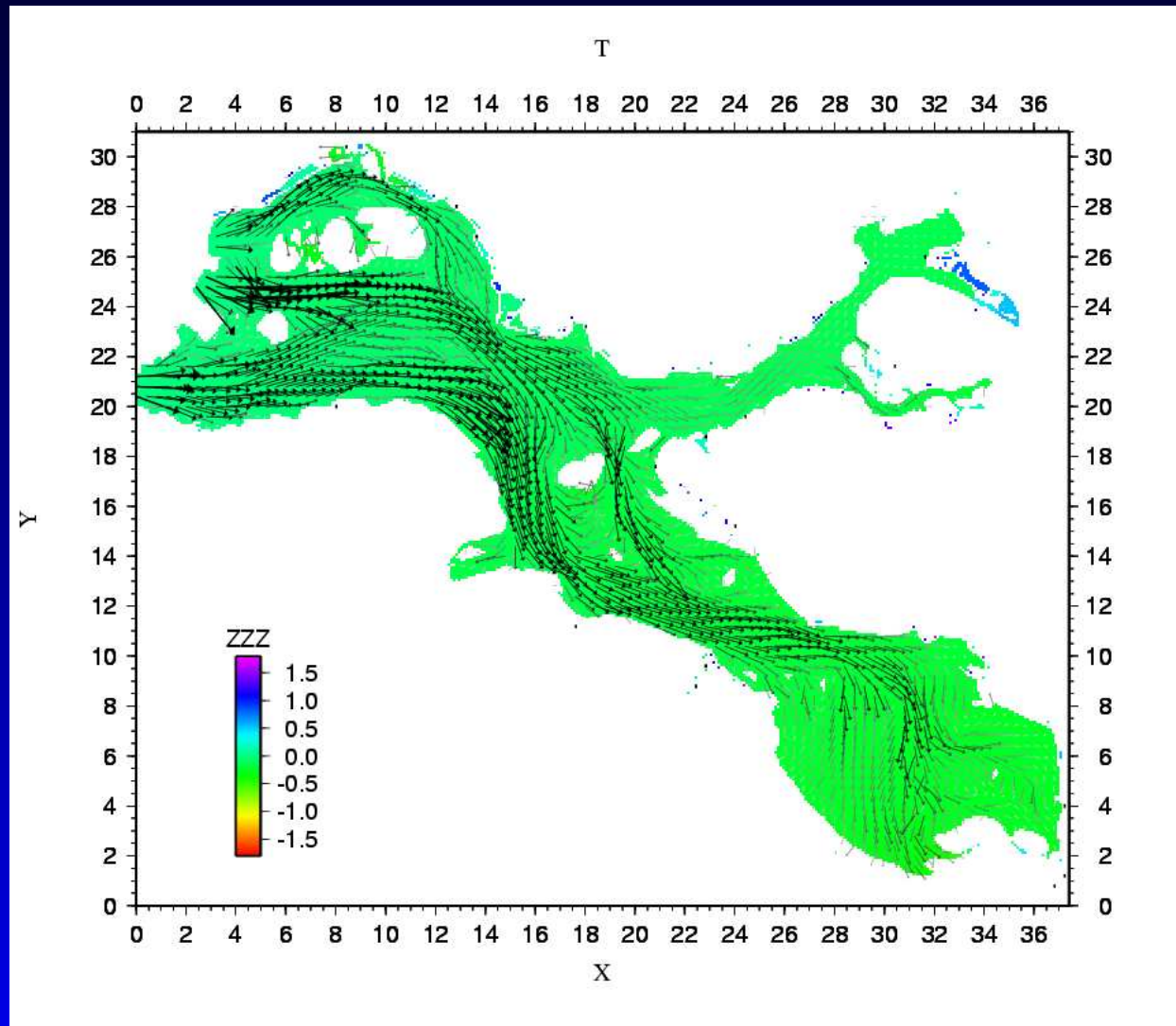
EU-Project MaBenE, Managing Benthic Ecosystems



Photograph by Luis Fernandes, Lisboa, Portugal

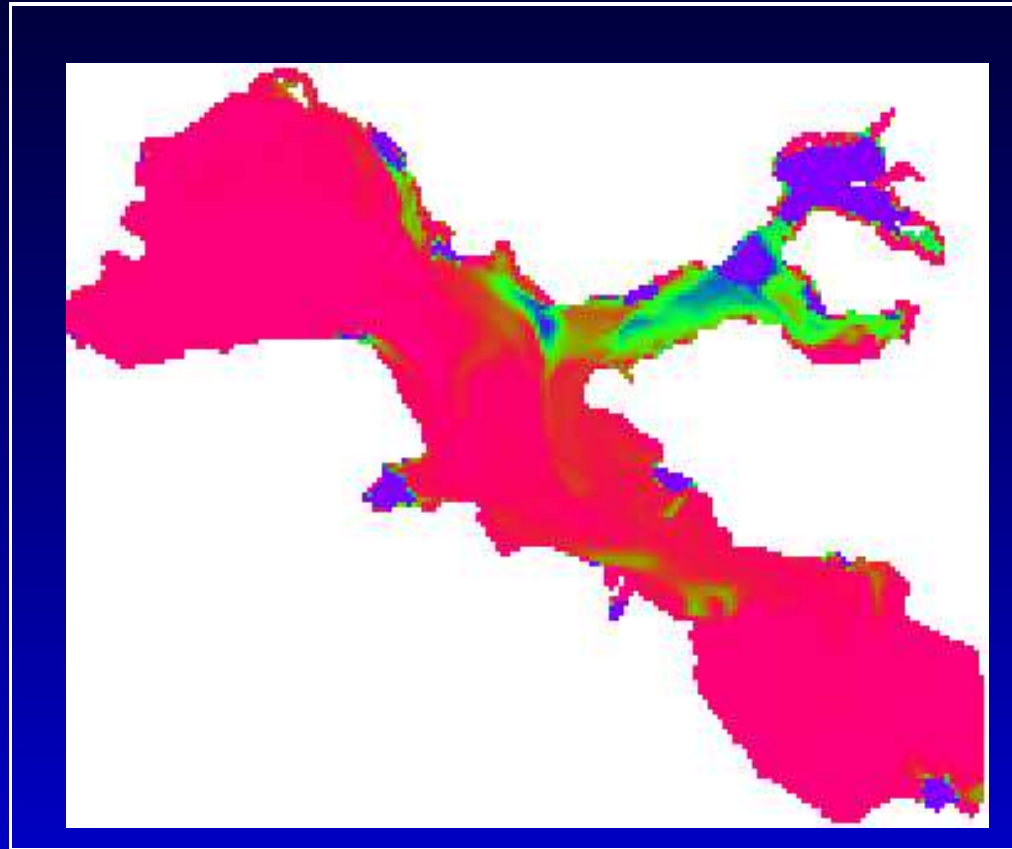
# Oosterschelde

## Full Flood



# Oosterschelde

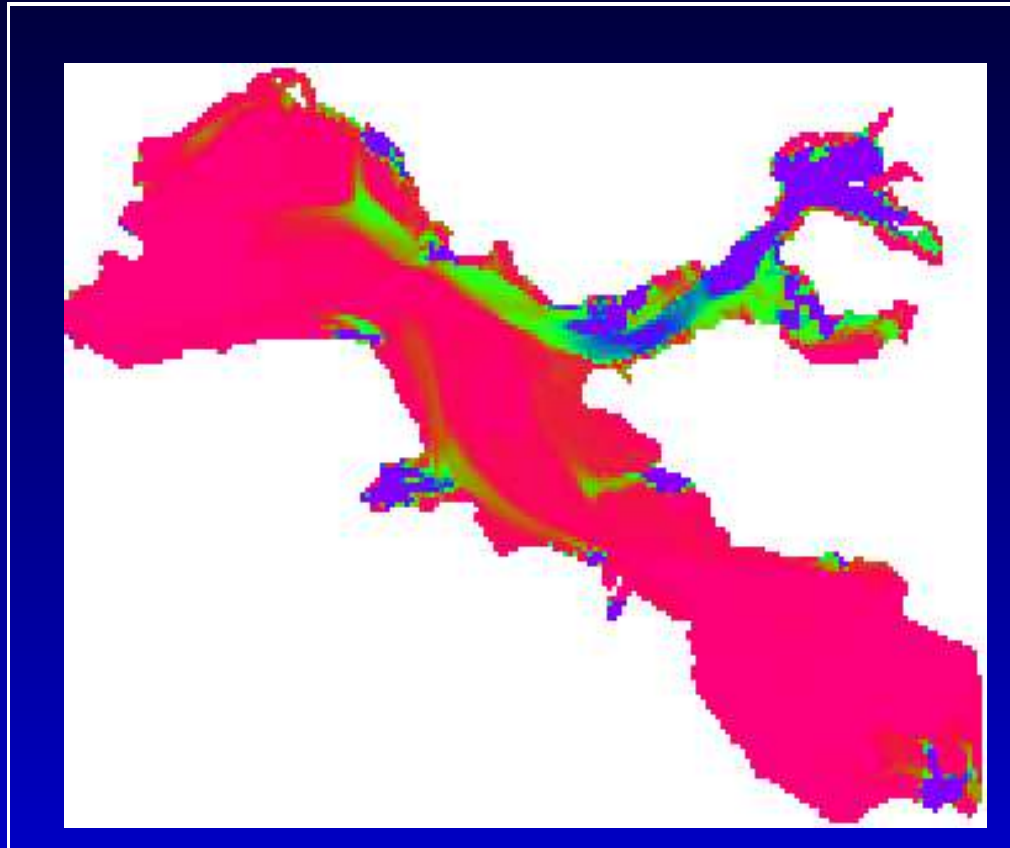
Surface salinity, Full Flood, Range 27 - 29 psu



Will freshwater release into the Wadden Sea lead to accumulation of fine sediments ?

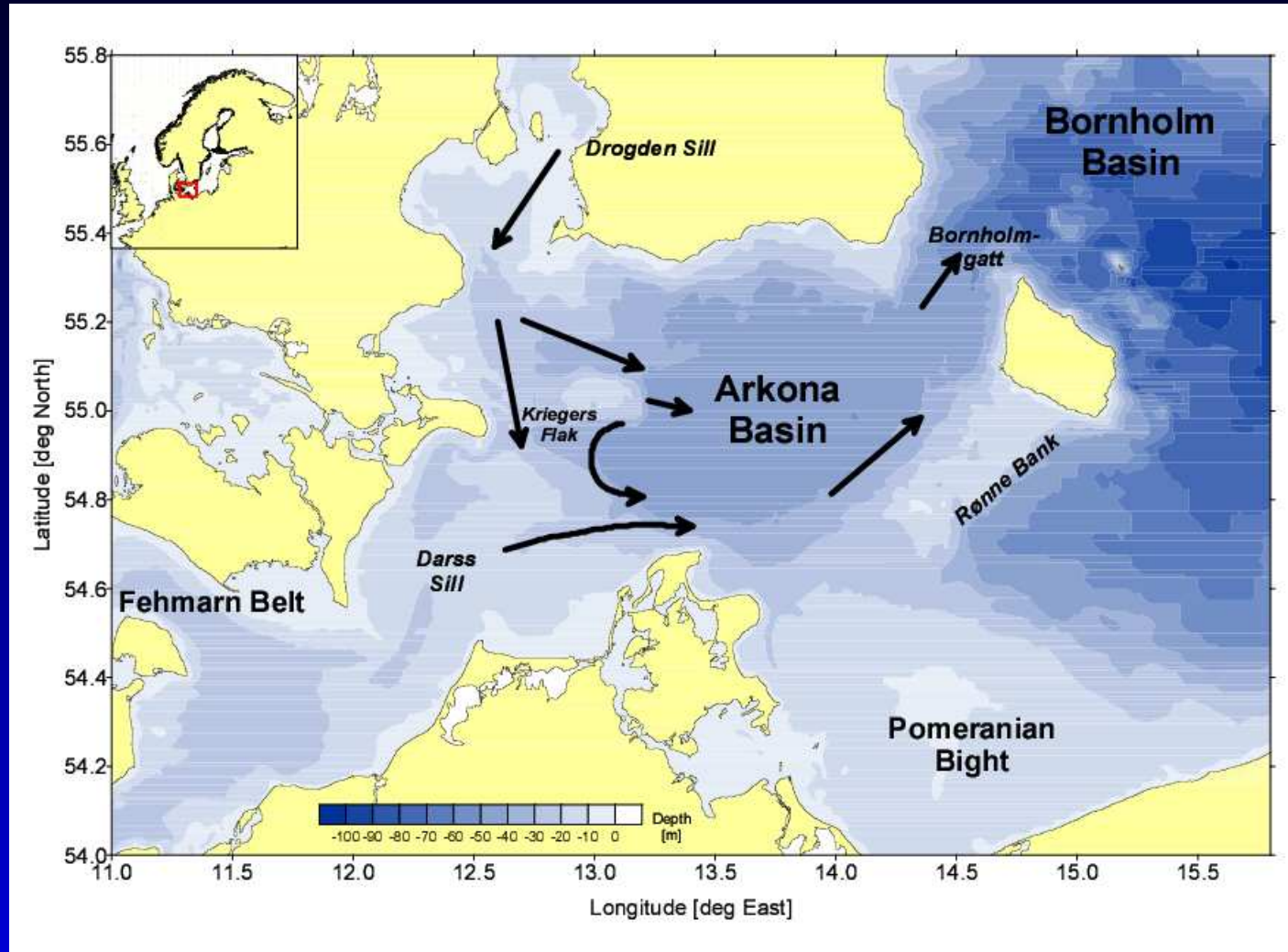
# Oosterschelde

Surface salinity, Full Ebb, Range 27 - 29 psu



Will freshwater release into the Wadden Sea lead to accumulation of fine sediments ?

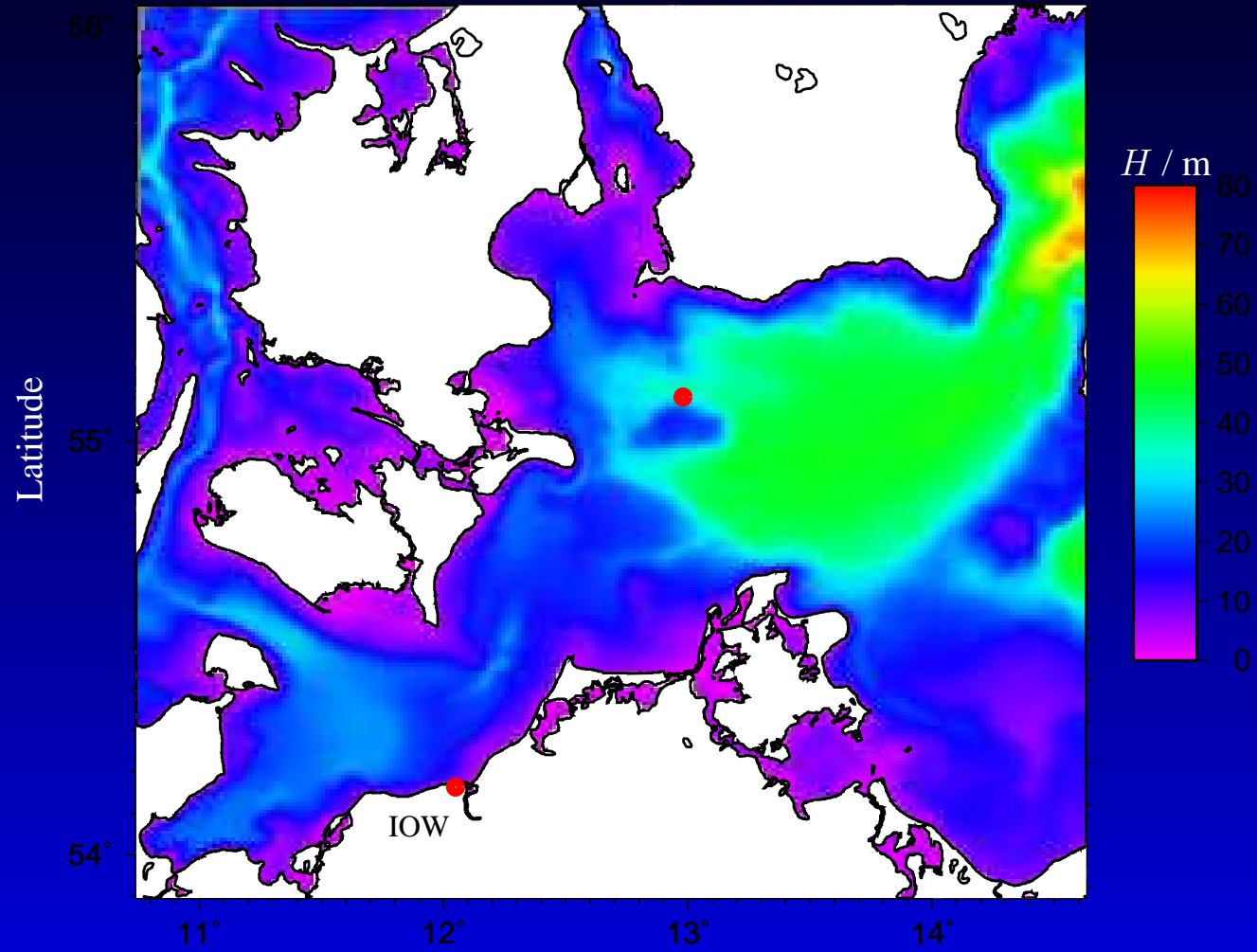
# Arkona Sea



Graphics by Volker Mohrholz, IOW

# Arkona Sea

Model bathymetry

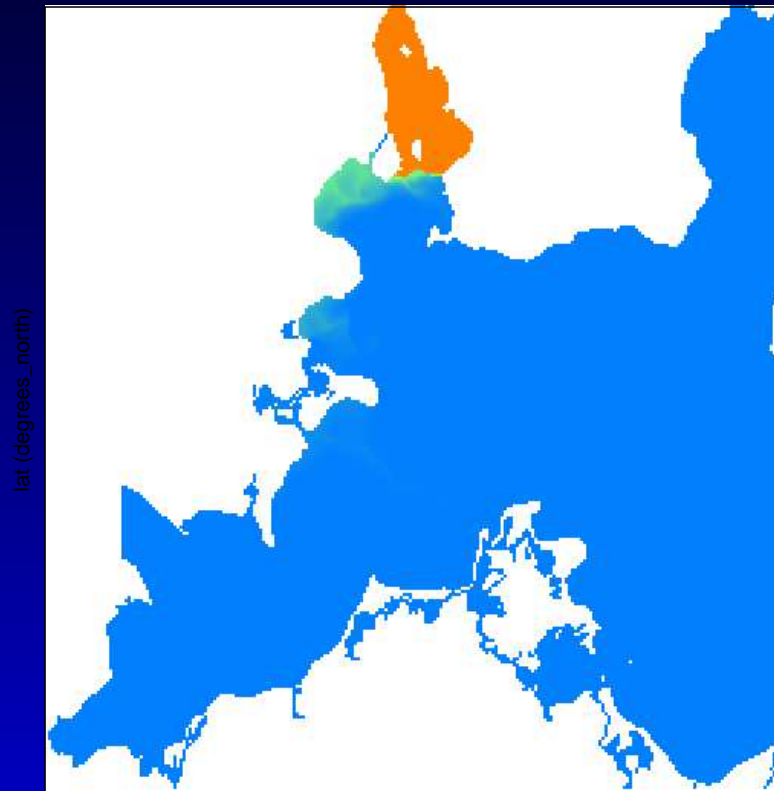


Longitude  
●: QuantAS station

# Arkona Sea

Surface salinity (8-25 psu)

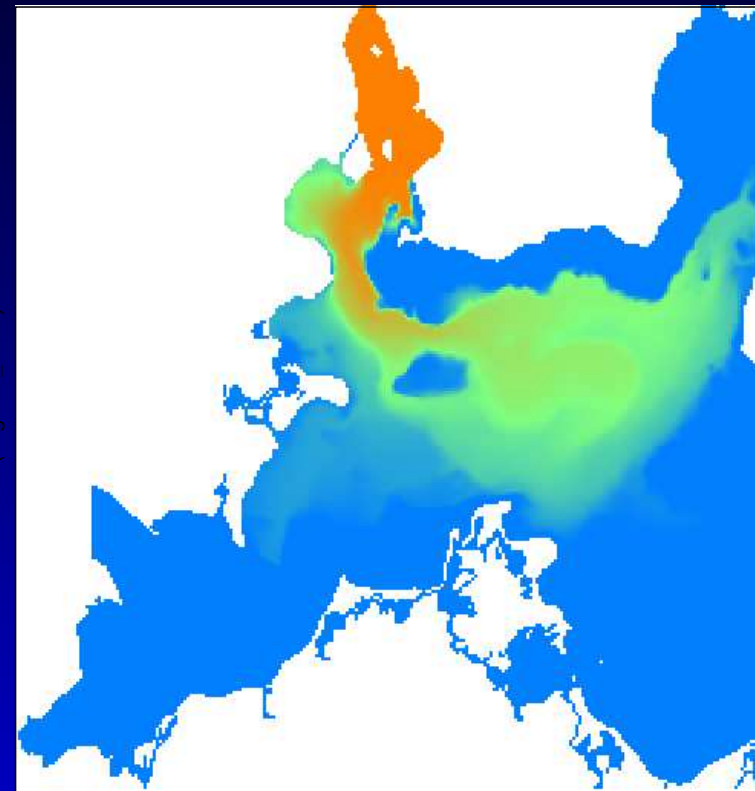
surface salinity (PSU)



lon (degrees\_east)

Bottom salinity (8-25 psu)

bottom salinity (PSU)

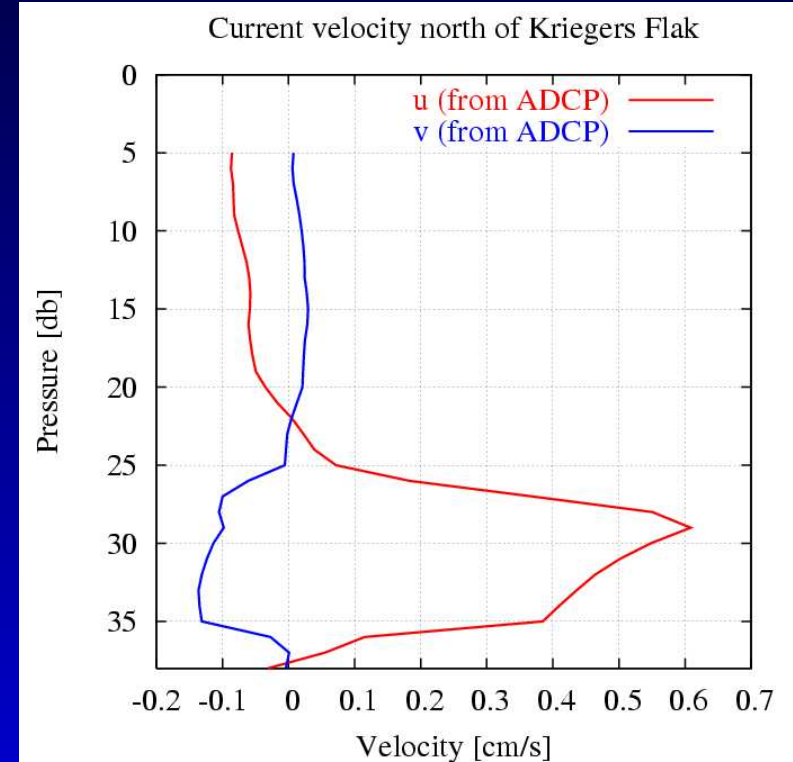
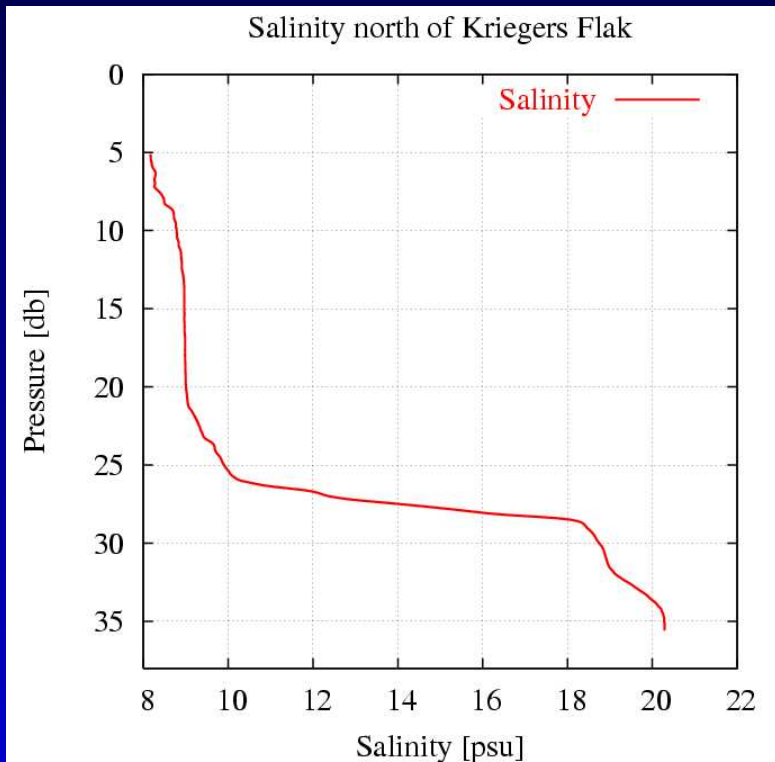


lon (degrees\_east)

Simulation with GETM

# Arkona Sea

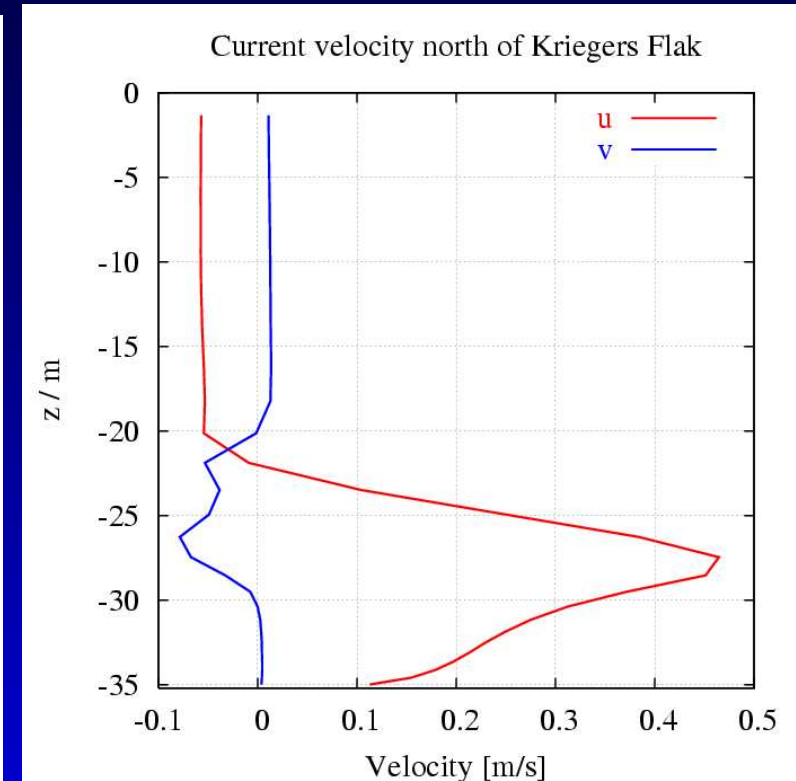
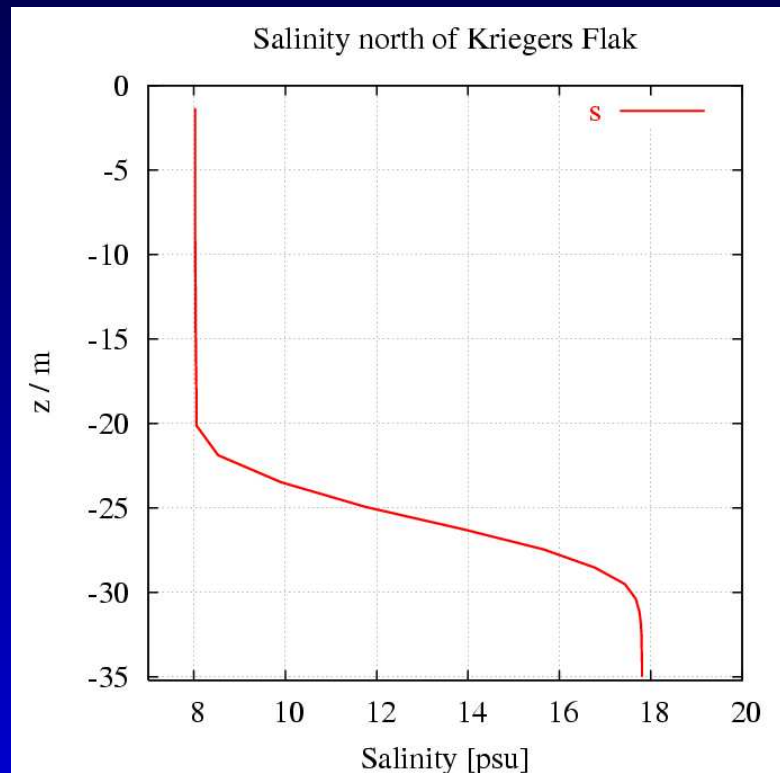
Observations from moored ship (MzB Helmsand)



Data by Jürgen Sellschopp, Volker Fiekas, FWG Kiel

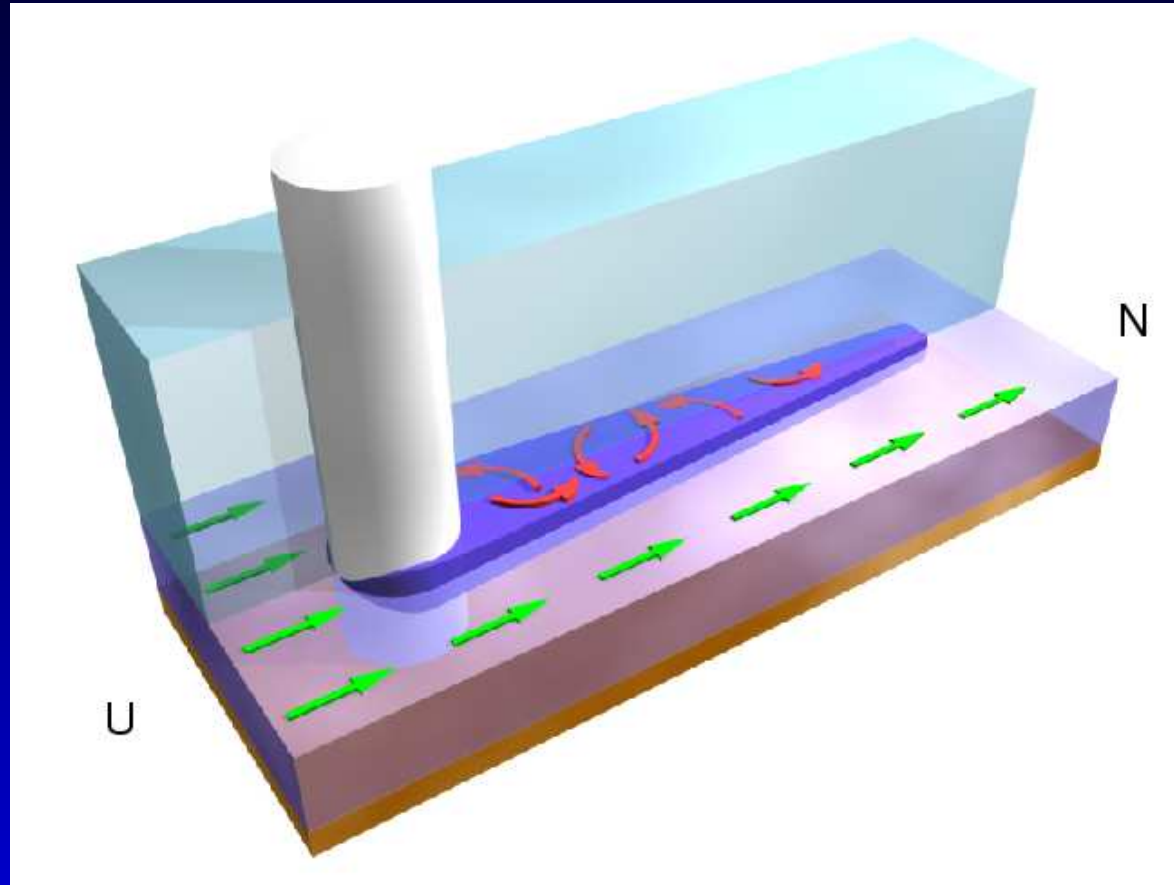
# Arkona Sea

Idealised simulations (with GETM)



# Offshore Constructions

Additional mixing by Offshore Wind Farms ?



Graphics by Jan Donath (IOW)

# Conclusions

Quantitative numerical simulations of buoyancy effects in the coastal zone require models with certain properties such as

- Higher turbulence closures
- Surface and bottom following coordinates
- Positive definite and monotone advection schemes

Advantageous are highly flexible vertical and horizontal coordinates.